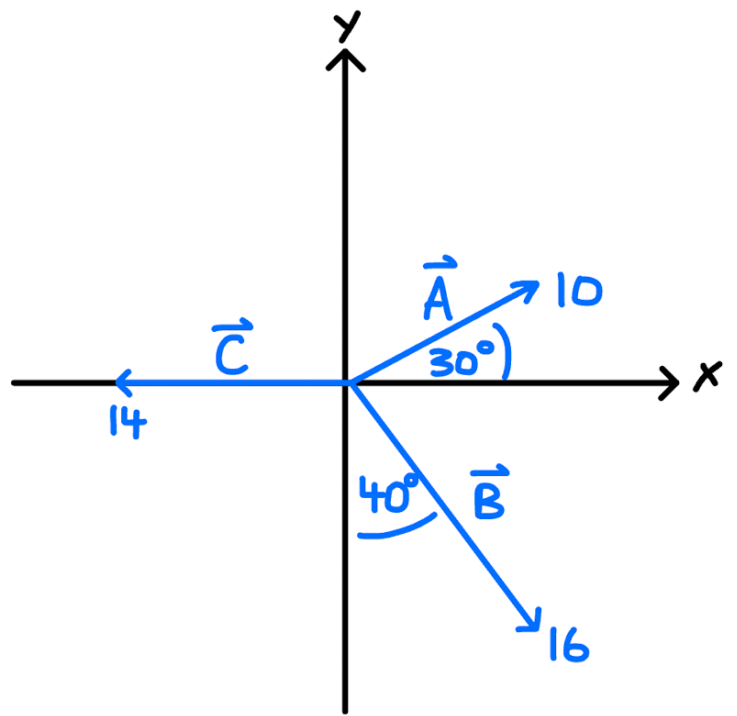
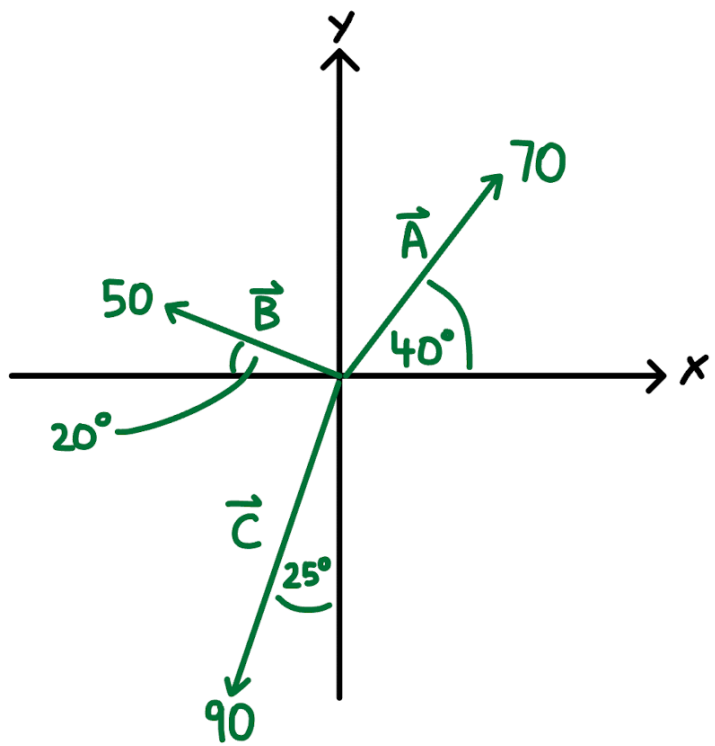


Determine  $\vec{A} + \vec{B} + \vec{C} = \vec{R}$



Determine  $\vec{A} + \vec{B} + \vec{C} = \vec{R}$



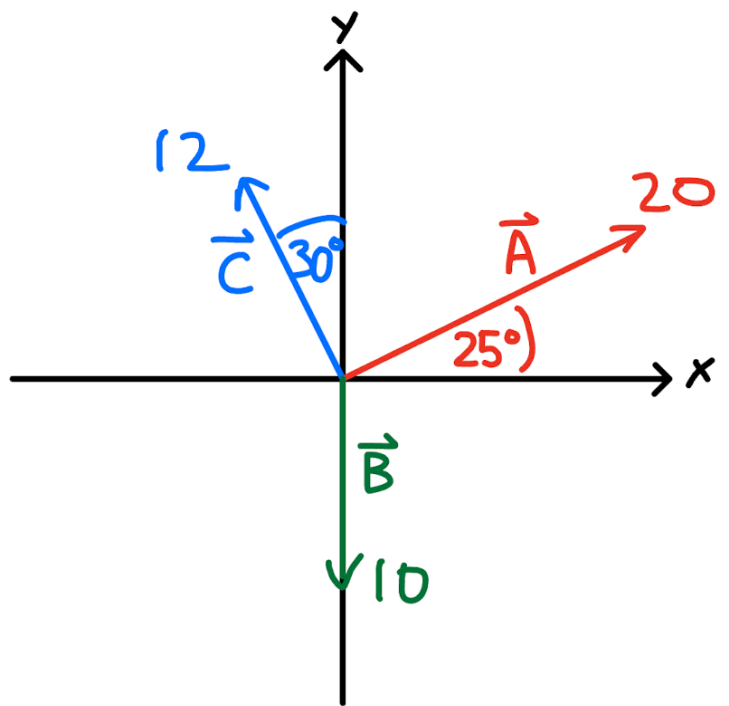
Determine

a)  $\vec{A} + \vec{B}$

b)  $\vec{A} - \vec{B}$

c)  $\vec{A} + \vec{C}$

d)  $\vec{A} + \vec{B} + \vec{C}$

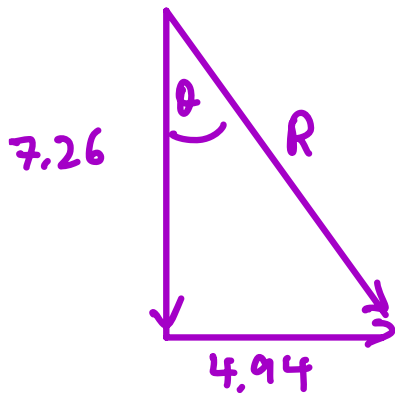
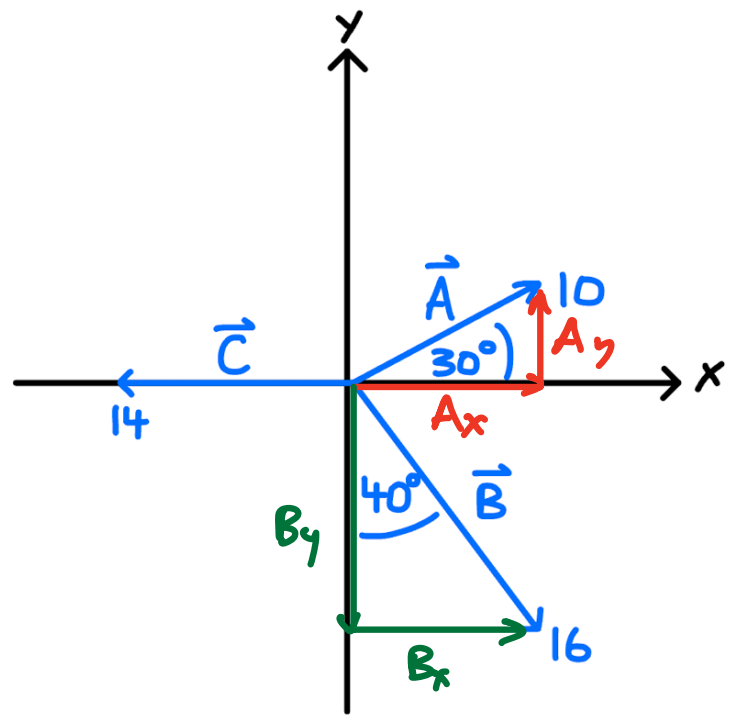


A plane has an air speed of 880 km/h and aims  $40^\circ$  west of south. Wind blows from the west at 80 km/h. What is the groundspeed of the plane? Direction?

A plane can travel at 700 km/h in still air. A 100 km/h wind blows  $30^\circ$  north of east. What direction should the plane aim to reach a destination directly to the east?

Determine  $\vec{A} + \vec{B} + \vec{C} = \vec{R}$

x	y
$A_x = +10 \cos 30^\circ$ $= +8.66$	$A_y = +10 \sin 30^\circ$ $= +5$
$B_x = +16 \sin 40^\circ$ $= +10.3$	$B_y = -16 \cos 40^\circ$ $= -12.3$
$C_x = -14$	$C_y = 0$
$R_x = +4.94$	$R_y = -7.26$



$$R = \sqrt{(4.94)^2 + (7.26)^2}$$

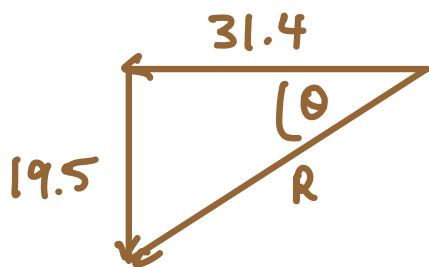
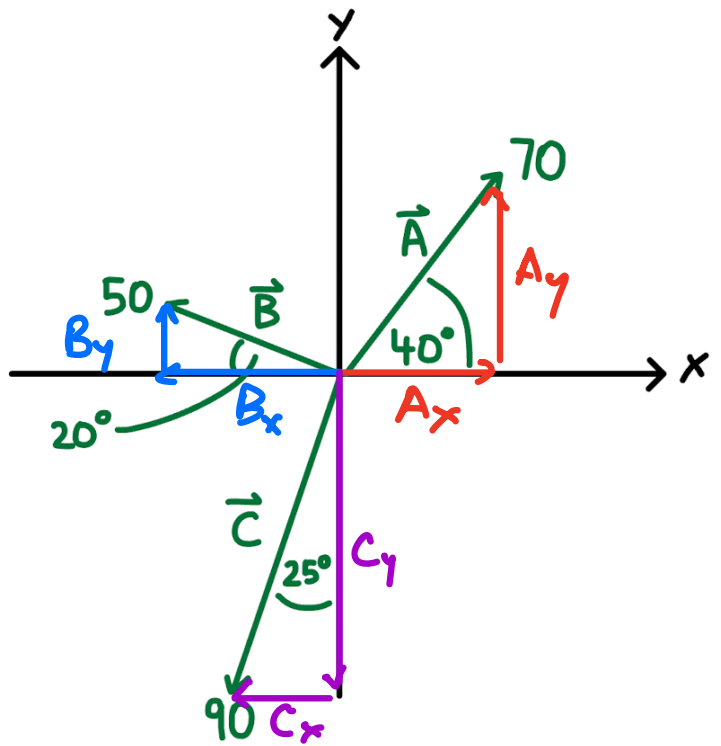
$$= 8.78$$

$$\theta = \tan^{-1}\left(\frac{4.94}{7.26}\right) = 34.3^\circ$$

8.78    34.3°    E of S

Determine  $\vec{A} + \vec{B} + \vec{C} = \vec{R}$

x	y
$A_x = +70 \cos 40^\circ$ $= +53.6$	$A_y = +70 \sin 40^\circ$ $= +45.0$
$B_x = -50 \cos 20^\circ$ $= -47.0$	$B_y = +50 \sin 20^\circ$ $= +17.1$
$C_x = -90 \sin 25^\circ$ $= -38.0$	$C_y = -90 \cos 25^\circ$ $= -81.6$
$R_x = -31.4$	$R_y = -19.5$



$$R = \sqrt{(31.4)^2 + (19.5)^2}$$

$$= 36.9$$

$$\theta = \tan^{-1} \left( \frac{19.5}{31.4} \right) = 31.8^\circ$$

36.9    31.8° S of W

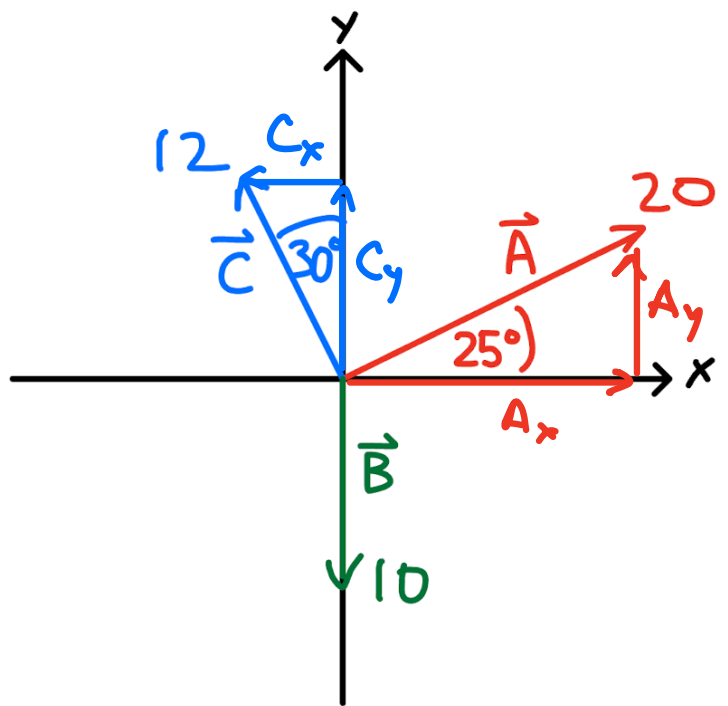
Determine

a)  $\vec{A} + \vec{B}$

b)  $\vec{A} - \vec{B}$

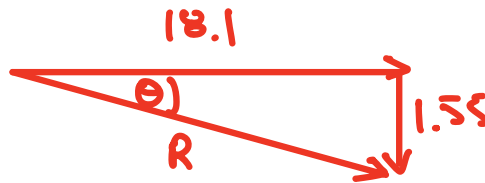
c)  $\vec{A} + \vec{C}$

d)  $\vec{A} + \vec{B} + \vec{C}$



x	y
$A_x = +20 \cos 25^\circ$ $= +18.1$	$A_y = +20 \sin 25^\circ$ $= +8.45$
$B_x = 0$	$B_y = -10$
$C_x = -12 \sin 30^\circ$ $= -6$	$C_y = +12 \cos 30^\circ$ $= +10.4$

a)  $R_x = A_x + B_x = +18.1$   
 $R_y = A_y + B_y = -1.55$



$$R = \sqrt{(18.1)^2 + (1.55)^2}$$

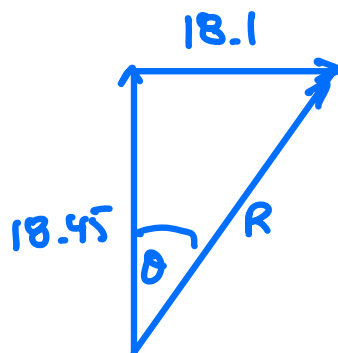
$$= 18.2$$

$$\theta = \tan^{-1}\left(\frac{1.55}{18.1}\right)$$

$$= 4.88^\circ$$

18.2    4.88° S of E

b)  $R_x = A_x - B_x = +18.1$   
 $R_y = A_y - B_y = +18.45$



$$R = \sqrt{(18.1)^2 + (18.45)^2}$$

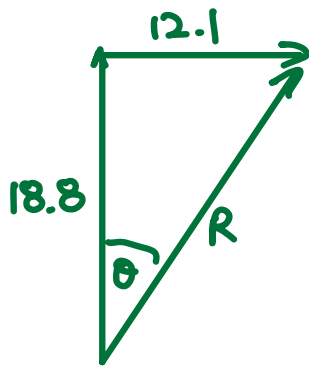
$$= 25.9$$

$$\theta = \tan^{-1}\left(\frac{18.1}{18.45}\right)$$

$$= 44.5^\circ$$

25.9    44.5° E of N

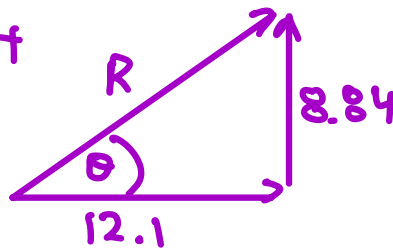
$$c) R_x = A_x + C_x = +12.1$$
$$R_y = A_y + C_y = +18.8$$



$$R = \sqrt{(12.1)^2 + (18.8)^2}$$
$$= 22.4$$
$$\theta = \tan^{-1}\left(\frac{12.1}{18.8}\right)$$
$$= 32.8^\circ$$

22.4	32.8° E of N
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$$d) R_x = A_x + B_x + C_x = +12.1$$
$$R_y = A_y + B_y + C_y = +8.84$$



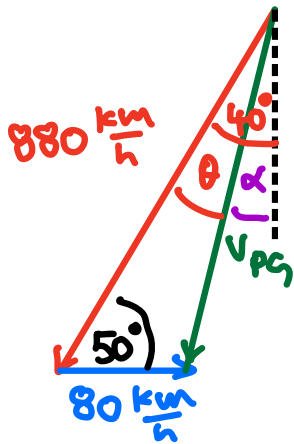
$$R = \sqrt{(12.1)^2 + (8.84)^2}$$
$$= 15.0$$
$$\theta = \tan^{-1}\left(\frac{8.84}{12.1}\right)$$
$$= 36.1^\circ$$

15.0	36.1° N of E
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A plane has an air speed of 880 km/h and aims 40° west of south. Wind blows from the west at 80 km/h. What is the groundspeed of the plane? Direction?

$$\vec{V}_{PA} + \vec{V}_{AG} = \vec{V}_{PG}$$



$$V_{PG}^2 = (880)^2 + (80)^2 - 2(880)(80)\cos 50^\circ$$

$$V_{PG} = 831 \frac{\text{km}}{\text{h}}$$

$$\frac{\sin \theta}{80} = \frac{\sin 50^\circ}{831}$$

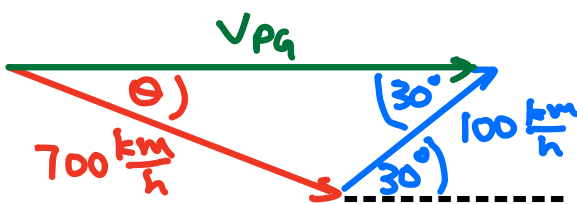
$$\theta = \sin^{-1}\left(\frac{80}{831} \sin 50^\circ\right) = 4.23^\circ$$

$$\alpha = 40^\circ - \theta = 40^\circ - 4.23^\circ = 35.8^\circ$$

$831 \frac{\text{km}}{\text{h}} \quad 35.8^\circ \quad \text{W of S}$

A plane can travel at 700 km/h in still air. A 100 km/h wind blows 30° north of east. What direction should the plane aim to reach a destination directly to the east?

$$\vec{V}_{PA} + \vec{V}_{AG} = \vec{V}_{PG}$$



$$\frac{\sin \theta}{100} = \frac{\sin 30^\circ}{700}$$

$$\theta = \sin^{-1}\left(\frac{100}{700} \sin 30^\circ\right)$$

$$= 4.10^\circ$$

$4.10^\circ \quad \text{S of E}$